

SCO INTERNATIONAL MATHS OLYMPIAD

CLASS 12 SAMPLE PAPER

Practice Paper with Answer Key & Explanations

SCO International Olympiad practice, assessment, reporting, and future-ready academic growth.

- relations, functions, algebra, calculus, vectors, 3D geometry, linear programming, and probability
- conceptual problem-solving with real-world modelling, proof logic, and multi-step calculations
- PDF-ready academic layout with compact question labels and explanations for transparent learning

Relations & Functions	Algebra	Calculus	Vectors & 3D	Probability
Matrices	Determinants	Integration	Differential Equations	Olympiad Reasoning

Sample Paper - Practice Edition

Class	12
Exam	SCO International Maths Olympiad
Question Paper Set	H
Academic Session	Sample / Practice
Total Questions	35
Time	60 minutes
Format	General Mathematics, Case Study, Assertion-Reason, Achievers Section

General Mathematics

Q1. If R is a relation on integers defined by aRb if a and b have the same parity, then R is:

- A. reflexive only
- B. symmetric only
- C. equivalence relation
- D. not transitive

Answer: C

Explanation: Same parity is reflexive, symmetric, and transitive; hence it is an equivalence relation.

Q2. The principal value of $\tan^{-1}(1)$ is:

- A. $\pi/6$
- B. $\pi/4$
- C. $\pi/3$
- D. $\pi/2$

Answer: B

Explanation: $\tan(\pi/4)=1$ and the principal value lies in $(-\pi/2, \pi/2)$.

Q3. If $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$, then A^2 equals:

- A. $\begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$
- B. $\begin{bmatrix} 2 & 1 \\ 0 & 2 \end{bmatrix}$
- C. $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$
- D. $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$

Answer: A

Explanation: Multiplying A by itself gives first row $[1,2]$ and second row $[0,1]$.

Q4. For the determinant $|x \ 1; 4 \ x| = 0$, find x .

- A. ± 1
- B. ± 2
- C. ± 4
- D. 0 only

Answer: B

Explanation: The determinant is $x^2 - 4$. Setting it to zero gives $x = \pm 2$.

Q5. Find $d/dx (\ln(\sin x))$.

- A. $\tan x$
- B. $\cot x$
- C. $\sec x$
- D. $\operatorname{cosec} x$

Answer: B

Explanation: $d/dx \ln(\sin x) = (\cos x)/(\sin x) = \cot x$.

Q6. If $y = e^{2x}$, then d^2y/dx^2 equals:

- A. e^{2x}
- B. $2e^{2x}$
- C. $4e^{2x}$
- D. $8e^{2x}$

Answer: C

Explanation: First derivative is $2e^{2x}$; differentiating again gives $4e^{2x}$.

Q7. Find the minimum value of $f(x)=x^2-6x+10$.

- A. 0
- B. 1
- C. 3
- D. 10

Answer: B

Explanation: $f(x)=(x-3)^2+1$, so the minimum value is 1.

Q8. Evaluate $\int (1/x) dx$ for $x>0$.

- A. x
- B. $\ln x + C$
- C. $1/x^2 + C$
- D. $e^x + C$

Answer: B

Explanation: The antiderivative of $1/x$ on $x>0$ is $\ln x + C$.

Q9. Evaluate $\int_0^\pi \sin x dx$.

- A. 0
- B. 1
- C. 2
- D. π

Answer: C

Explanation: $\int \sin x dx = -\cos x$. From 0 to π : $-\cos\pi - (-\cos 0) = 1 + 1 = 2$.

Q10. Area under $y = 2x$ from $x = 0$ to $x = 3$ is:

- A. 3
- B. 6
- C. 9
- D. 12

Answer: C

Explanation: Area = $\int_0^3 2x dx = [x^2]_0^3 = 9$.

Q11. The solution of $dy/dx = 2x$ with $y(1)=5$ is:

- A. $y=x^2+4$
- B. $y=2x^2+3$
- C. $y=x+4$
- D. $y=5x^2$

Answer: A

Explanation: Integrating gives $y=x^2+C$. Using $y(1)=5$ gives $C=4$.

Q12. For $a=(2, 1, -2)$, find $|a|$.

- A. 2
- B. 3
- C. 4
- D. 5

Answer: B

Explanation: $|a|=\sqrt{(2^2+1^2+(-2)^2)}=\sqrt{9}=3$.

Q13. Direction ratios of the line joining A(1,2,3) and B(3,5,7) are:

- A. (1,2,3)
- B. (2,3,4)
- C. (3,5,7)
- D. (4,3,2)

Answer: B

Explanation: $B-A=(3-1,5-2,7-3)=(2,3,4)$.

Q14. The feasible region of a linear programming problem is bounded. Which statement is true?

- A. An optimum can occur only inside the region
- B. An optimum occurs at a corner point if it exists
- C. No optimum is possible
- D. Every point gives the same value

Answer: B

Explanation: For a linear objective over a bounded polygonal region, the optimum occurs at one or more corner points.

Q15. If $P(A)=0.4$, $P(B)=0.5$ and A and B are independent, then $P(A \cap B)$ is:

- A. 0.1
- B. 0.2
- C. 0.4
- D. 0.9

Answer: B

Explanation: For independent events, $P(A \cap B)=P(A)P(B)=0.4 \times 0.5=0.2$.

Q16. If A is a square matrix and $A^2 = I$, then A^{-1} equals:

- A. A
- B. I
- C. $-A$
- D. A^2

Answer: A

Explanation: $A^2=I$ means $A \cdot A=I$, so A is its own inverse.

Q17. Find the derivative of $\sin(3x)$.

- A. $\cos(3x)$
- B. $3\cos(3x)$
- C. $-3\cos(3x)$
- D. $3\sin(3x)$

Answer: B

Explanation: By chain rule, $d/dx \sin(3x)=3\cos(3x)$.

Q18. Evaluate $\int_0^1 (x+1)^2 dx$.

- A. $4/3$
- B. $7/3$
- C. 2
- D. 3

Answer: B

Explanation: $(x+1)^2=x^2+2x+1$. Integral from 0 to 1 is $1/3+1+1=7/3$.

Q19. A fair die is thrown twice. What is the probability that the sum is 7?

- A. $1/12$
- B. $1/9$
- C. $1/6$
- D. $1/3$

Answer: C

Explanation: Favourable ordered pairs are (1,6),(2,5),(3,4),(4,3),(5,2),(6,1): 6 out of 36, so probability = $1/6$.

Q20. The angle between the planes $x+y+z=1$ and $x-y+z=2$ depends on the angle between their normals. What is the dot product of the normals?

- A. 0
- B. 1
- C. 2
- D. 3

Answer: B

Explanation: Normals are (1,1,1) and (1,-1,1). Their dot product is $1-1+1=1$.

Case Study

Q21. Case: A bank models an investment by $A(t)=10000e^{0.05t}$. What is the instantaneous rate of growth at $t=0$?

- A. 50
- B. 100
- C. 500
- D. 10000

Answer: C

Explanation: $A'(t)=0.05 \times 10000e^{0.05t}=500e^{0.05t}$. At $t=0$, the rate is 500.

Q22. Case: A drone's position is $r(t)=(t, t^2, 2t)$. What is its velocity vector at $t=2$?

- A. (1,2,2)
- B. (1,4,2)
- C. (2,4,4)
- D. (4,1,2)

Answer: B

Explanation: Velocity is $r'(t)=(1,2t,2)$. At $t=2$, it is (1,4,2).

Q23. Case: A manufacturer produces x units of Product A and y units of Product B with $x+y \leq 10$, $x \leq 7$, $y \leq 6$, $x,y \geq 0$. Which point is feasible?

- A. (8,3)
- B. (7,4)
- C. (5,5)
- D. (4,7)

Answer: C

Explanation: (5,5) satisfies $x+y=10$, $x \leq 7$, $y \leq 6$, and non-negativity. The other options violate at least one constraint.

Q24. Case: A survey finds that 30% of students take Maths, 20% take Physics, and 10% take both. What is the probability that a randomly chosen student takes Maths or Physics?

- A. 0.30
- B. 0.40

- C. 0.50
- D. 0.60

Answer: B

Explanation: $P(M \cup P) = P(M) + P(P) - P(M \cap P) = 0.30 + 0.20 - 0.10 = 0.40$.

Q25. Case: A water tank empties according to $dV/dt = -4$ for V in litres and t in minutes. If $V(0) = 100$, when will the tank be empty?

- A. 20 min
- B. 25 min
- C. 30 min
- D. 40 min

Answer: B

Explanation: $V = 100 - 4t$. Setting $V = 0$ gives $t = 25$ minutes.

Assertion-Reason

Q26. Assertion (A): The derivative of a constant function is zero. Reason (R): A constant function has no change in output as x changes.

- A. A and R are true, and R explains A
- B. A and R are true, but R does not explain A
- C. A is true, R is false
- D. A is false, R is true

Answer: A

Explanation: The rate of change of a constant function is zero, so the reason explains the assertion.

Q27. Assertion (A): For independent events A and B, $P(A|B) = P(A)$, provided $P(B) > 0$. Reason (R): B occurring does not alter the likelihood of A.

- A. A and R are true, and R explains A
- B. A and R are true, but R does not explain A
- C. A is true, R is false
- D. A is false, R is true

Answer: A

Explanation: This is the conditional-probability meaning of independence.

Q28. Assertion (A): The cross product of two parallel vectors is the zero vector. Reason (R): The sine of the angle between parallel vectors is zero.

- A. A and R are true, and R explains A
- B. A and R are true, but R does not explain A
- C. A is true, R is false
- D. A is false, R is true

Answer: A

Explanation: $|a \times b| = |a||b|\sin\theta$. For parallel vectors, $\theta = 0$ or π , so $\sin\theta = 0$.

Q29. Assertion (A): Every square matrix has an inverse. Reason (R): A matrix with determinant zero is singular.

- A. A and R are true, and R explains A
- B. A and R are true, but R does not explain A
- C. A is true, R is false
- D. A is false, R is true

Answer: D

Explanation: Not every square matrix is invertible; only non-singular matrices are. The reason is true.

Q30. Assertion (A): The area under a curve can be found by a definite integral. Reason (R): Integration is the inverse process of differentiation.

- A. A and R are true, and R explains A
- B. A and R are true, but R does not explain A
- C. A is true, R is false
- D. A is false, R is true

Answer: B

Explanation: Both statements are true, but the reason alone does not directly explain the geometric area interpretation.

Achievers Section

Q31. Find the value of $\int_0^1 x^2(1-x) dx$.

- A. 1/12
- B. 1/10
- C. 1/6
- D. 1/4

Answer: A

Explanation: $\int_0^1 (x^2 - x^3) dx = 1/3 - 1/4 = 1/12$.

Q32. If $\det(A) = -2$ for a 3×3 matrix, then $\det(-A)$ equals:

- A. -2
- B. 2
- C. 6
- D. -6

Answer: B

Explanation: For a 3×3 matrix, $\det(kA) = k^3 \det(A)$. $\det(-A) = -1^3 \times (-2) = 2$.

Q33. Find the shortest distance from the origin to the plane $3x + 4y - 12 = 0$.

- A. 12/5
- B. 5/12
- C. 3
- D. 4

Answer: A

Explanation: Distance = $| -12 | / \sqrt{3^2 + 4^2 + 0^2} = 12/5$.

Q34. If X has binomial distribution with $n=4$ and $p=1/2$, find $P(X=2)$.

- A. 1/8
- B. 3/8
- C. 1/2
- D. 5/8

Answer: B

Explanation: $P(X=2) = C(4,2)(1/2)^2(1/2)^2 = 6/16 = 3/8$.

Q35. The function $f(x) = x^3 - 6x^2 + 9x$ has local extrema at:

- A. $x=0$ and $x=3$
 B. $x=1$ and $x=3$
 C. $x=1$ and $x=4$
 D. $x=2$ only

Answer: B

Explanation: $f'(x)=3x^2-12x+9=3(x-1)(x-3)$, so critical points are $x=1$ and $x=3$.

Answer Key

Q	Ans	Q	Ans	Q	Ans	Q	Ans	Q	Ans
1	C	2	B	3	A	4	B	5	B
6	C	7	B	8	B	9	C	10	C
11	A	12	B	13	B	14	B	15	B
16	A	17	B	18	B	19	C	20	B
21	C	22	B	23	C	24	B	25	B
26	A	27	A	28	A	29	D	30	B
31	A	32	B	33	A	34	B	35	B